

# On-line Multi-label Classification

A Problem Transformation Approach

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# Outline

- Multi-label Classification
- Problem Transformation
  - Binary Method
  - Combination Method
- Pruned Sets Method (PS)
- Results
- On-line Applications
- Summary

# Multi-label Classification

- Single-label Classification
  - Set of instances, set of labels
  - Assign one label to each instance
  - e.g. "Shares plunge on financial fears", Economy

# Multi-label Classification

- Single-label Classification
  - Set of instances, set of labels
  - Assign one label to each instance
  - e.g. "Shares plunge on financial fears", Economy
- Multi-label Classification
  - Set of instances, set of labels
  - Assign **a subset of labels** to each instance
  - e.g. "Germany agrees bank rescue", {Economy, Germany}

# Applications

- Text Classification:
  - News articles; Encyclopedia articles; Academic papers; Web directories; E-mail; Newsgroups
- Images, Video, Music:
  - Scene classification; Genre classification
- Other:
  - Medical classification; Bioinformatics

N.B. Not the same as *tagging / keywords*.

# Multi-label Issues

- Relationships between labels
  - e.g. consider: {US, Iraq} VS {Iraq, Antarctica}
- Extra dimension
  - Imbalances exaggerated
  - Extra complexity
- Evaluation methods
  - Evaluate by label? by example?
- How to do Multi-label Classification?

# Problem Transformation

1. Transform multi-label data into single-label data
  2. Use one or more single-label classifiers
  3. Transform classifications back into multi-label representation
- Can employ *any* single-label classifier
    - *Naive Bayes, SVMs, Decision Trees, etc, ...*
  - *e.g. Binary Method, Combination Method, ..*  
*(overview by (Tsoumakas & Katakis, 2005))*

# Algorithm Transformation

1. Adapts a single-label algorithm to make multi-label classifications
2. Runs directly on multi-label data
  - Specific to a particular type of classifier
  - Does some form of *Problem Transformation* internally
  - *e.g. To AdaBoost* (Schapire & Singer, 2000), *Decision Trees* (Blockheer et al. 2008), *kNN* (Zhang & Zhou. 2005), *NB* (McCallum. 1999), ...



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# Binary Method

- One binary classifier for each label
- A label is either relevant or !relevant

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- A label is either relevant or !relevant

## *Multi-label Train*

$$L = \{A, B, C, D\}$$

d0, {A, D}

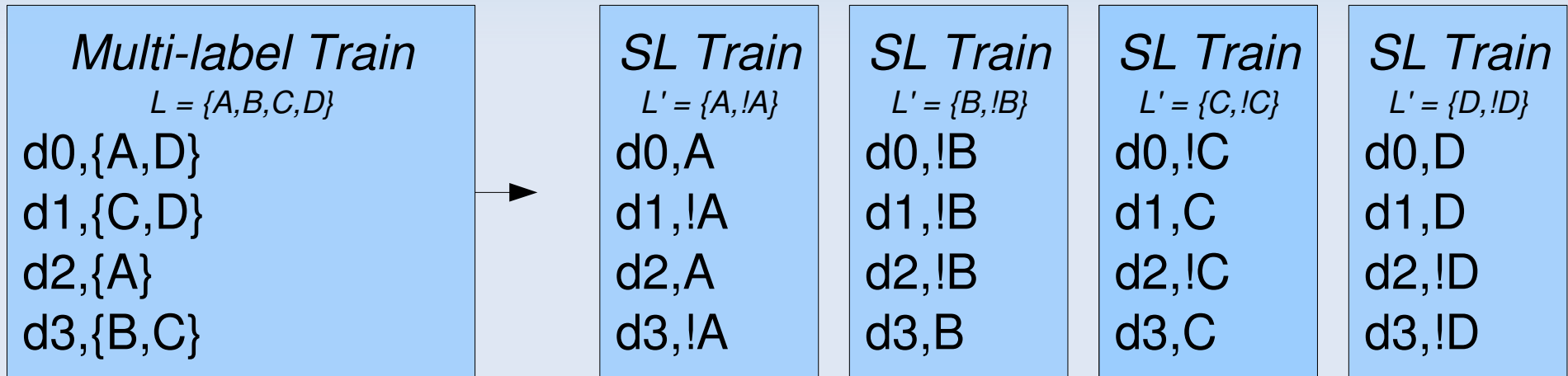
d1, {C, D}

d2, {A}

d3, {B, C}

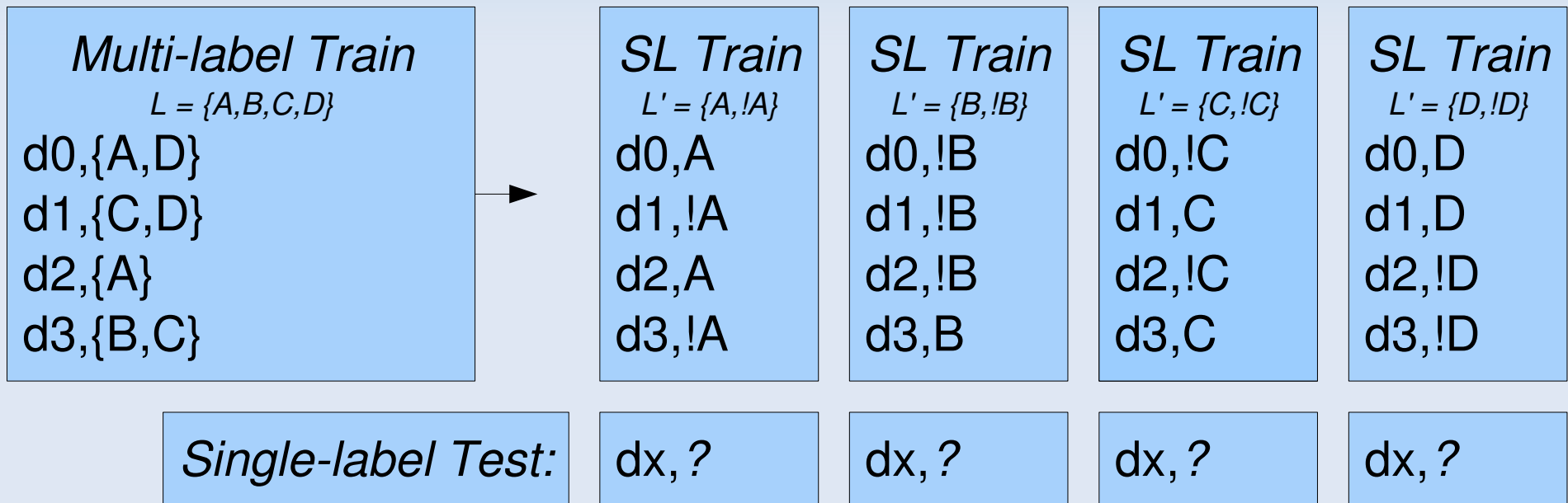
# Binary Method

- One binary classifier for each label
- A label is either relevant or !relevant



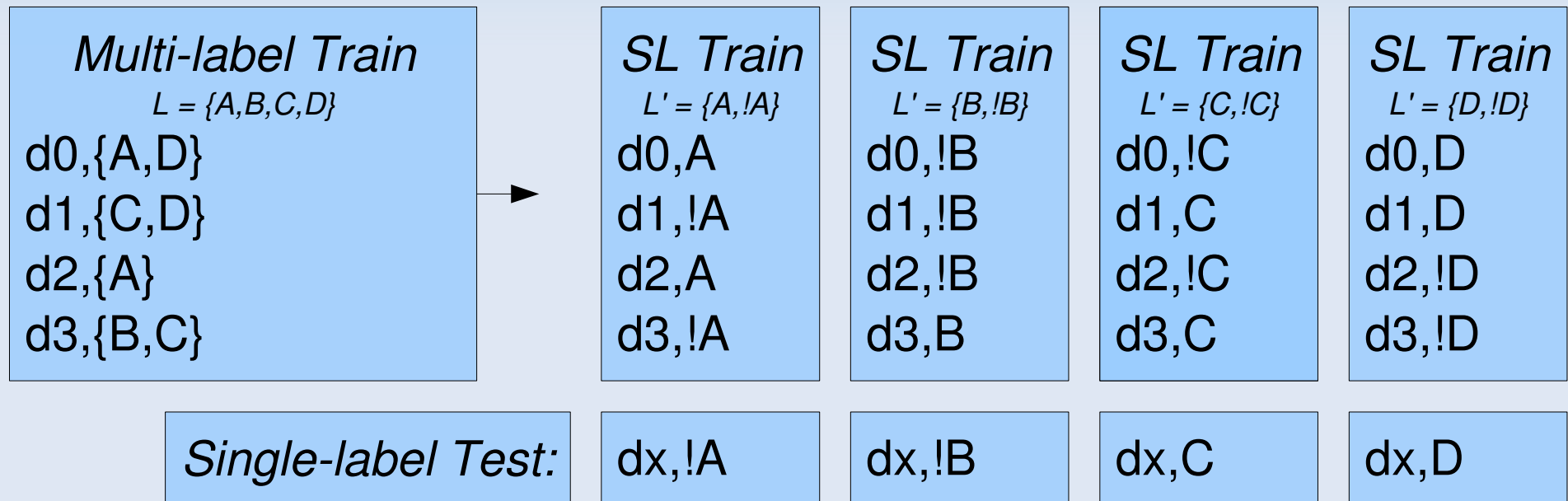
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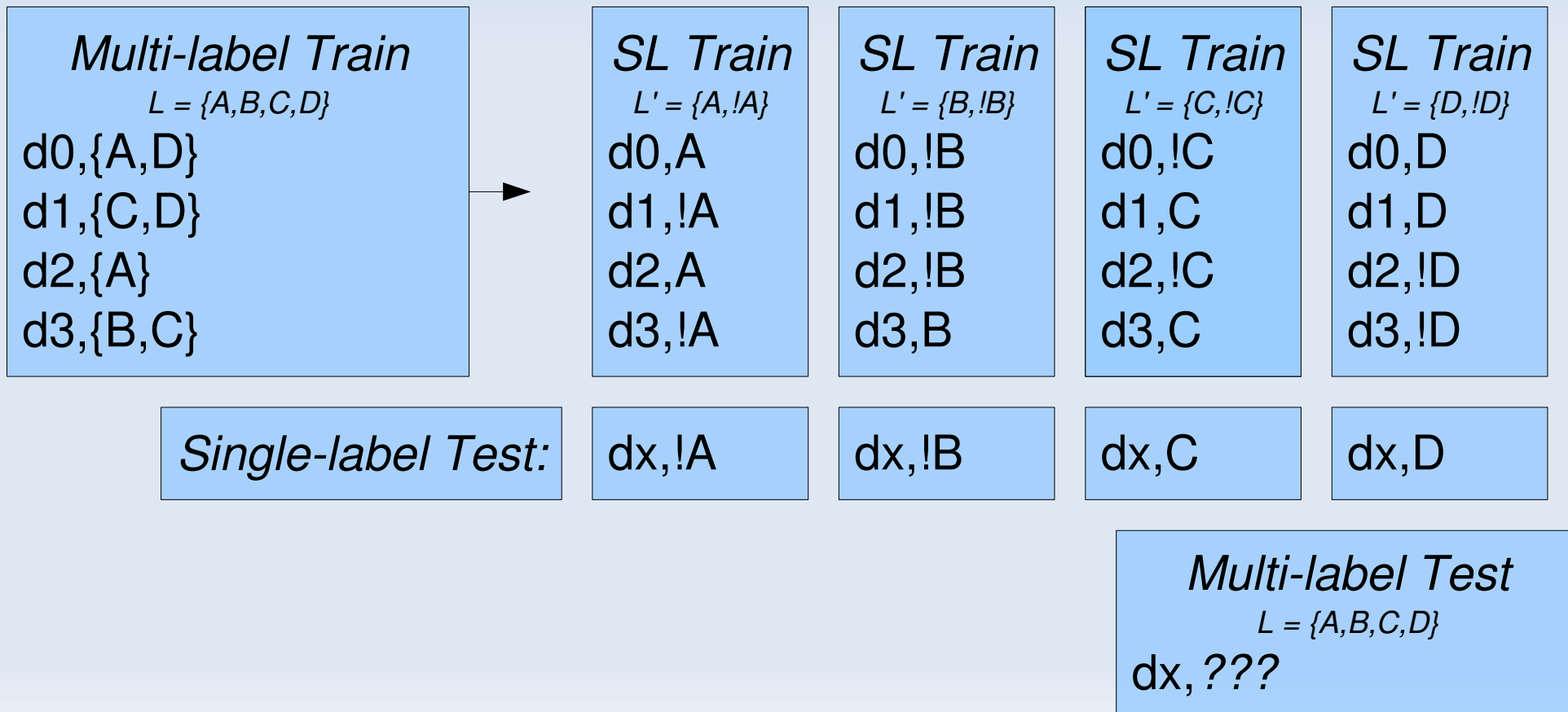
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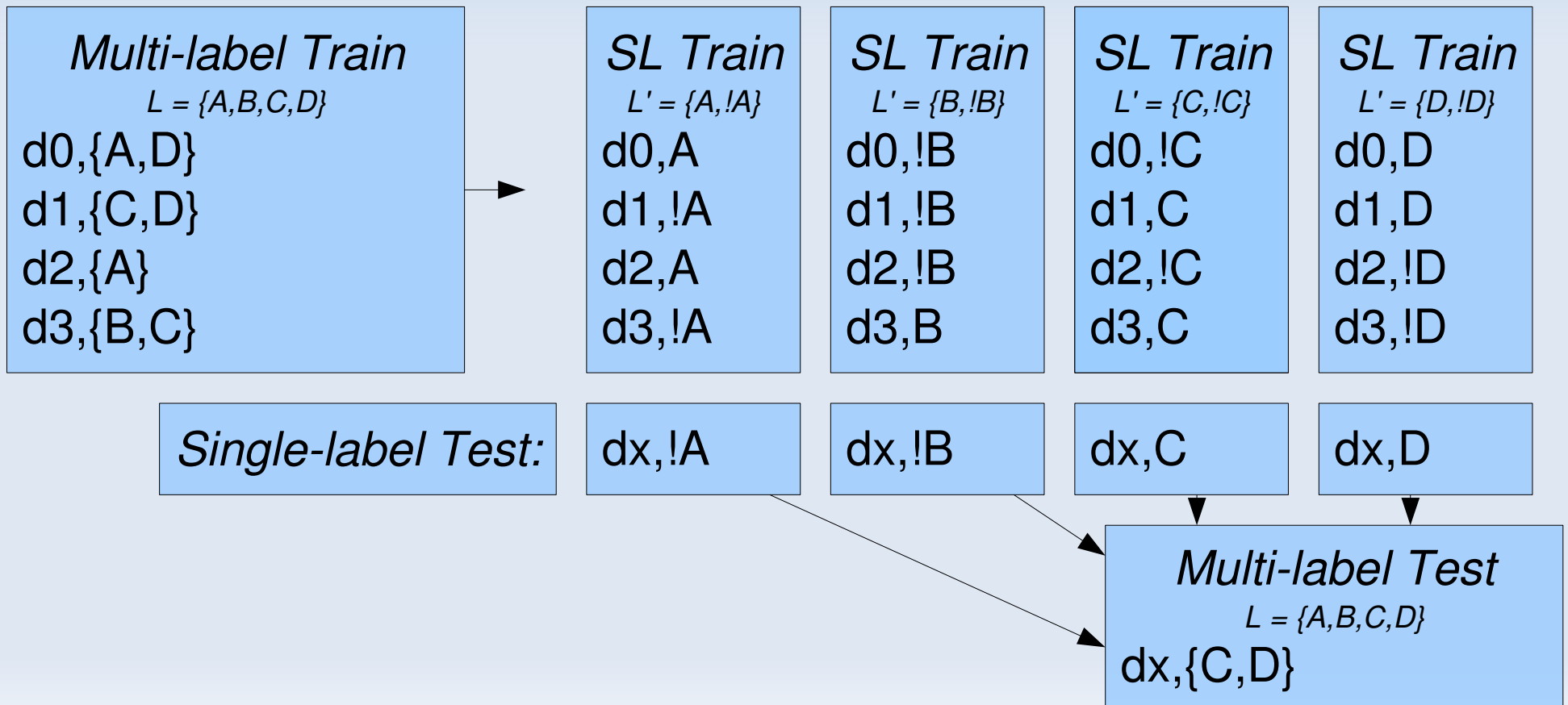
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# Binary Method

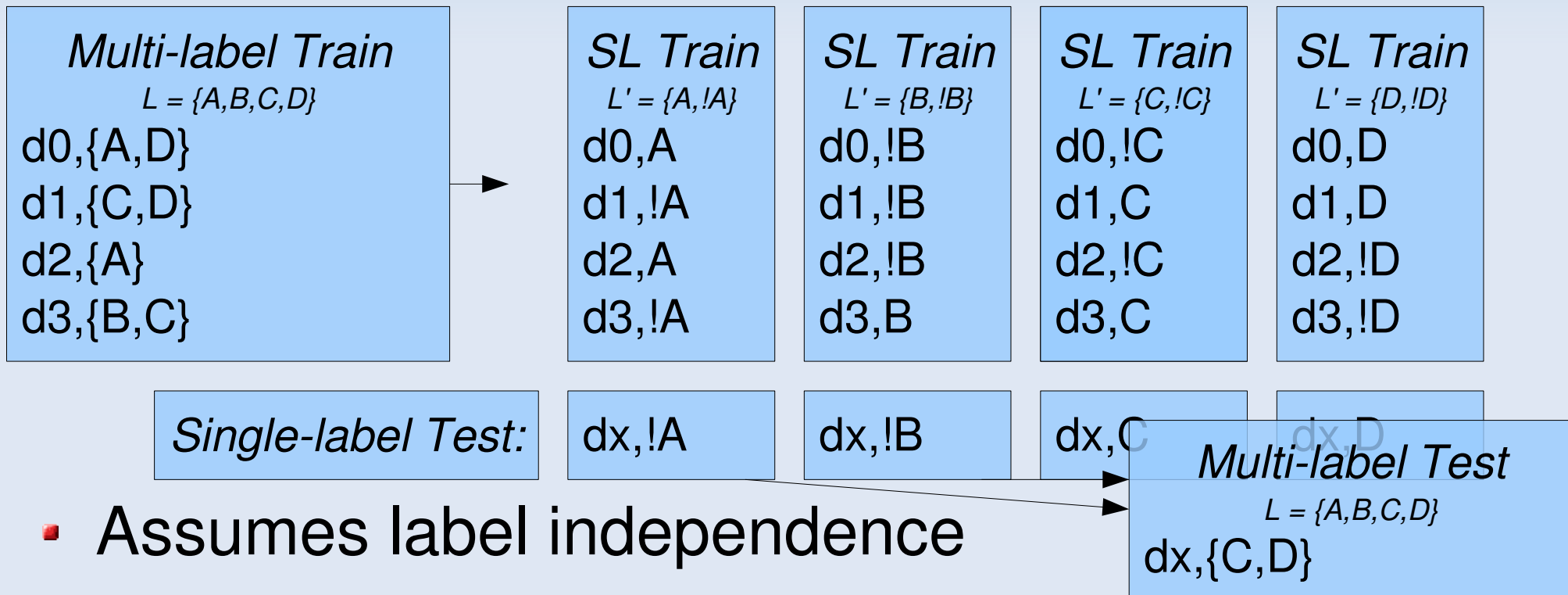
- One binary classifier for each label
- A label is either relevant or !relevant





# Binary Method

- One binary classifier for each label
- A label is either relevant or !relevant



- Assumes label independence
- Often unbalanced by many negative examples

# Combination Method

- One decision involves multiple labels
- Each subset becomes a single label

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- Each subset becomes a single label

## *Multi-label Train*

$$L = \{A, B, C, D\}$$

d0, {A, D}

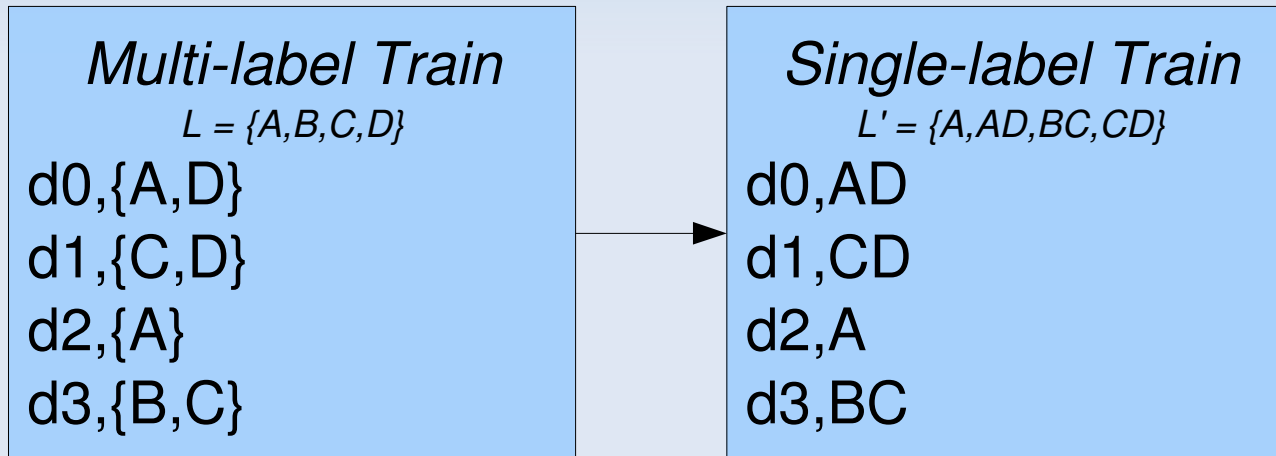
d1, {C, D}

d2, {A}

d3, {B, C}

# Combination Method

- One decision involves multiple labels
- Each subset becomes a single label



# Combination Method

- One decision involves multiple labels
- Each subset becomes a single label



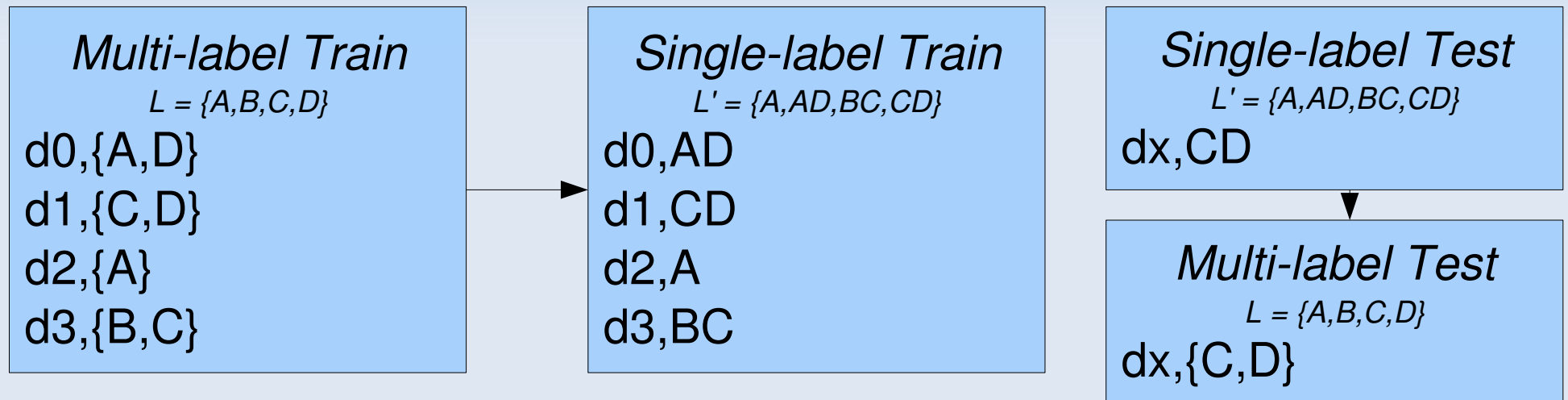
# Combination Method

- One decision involves multiple labels
- Each subset becomes a single label



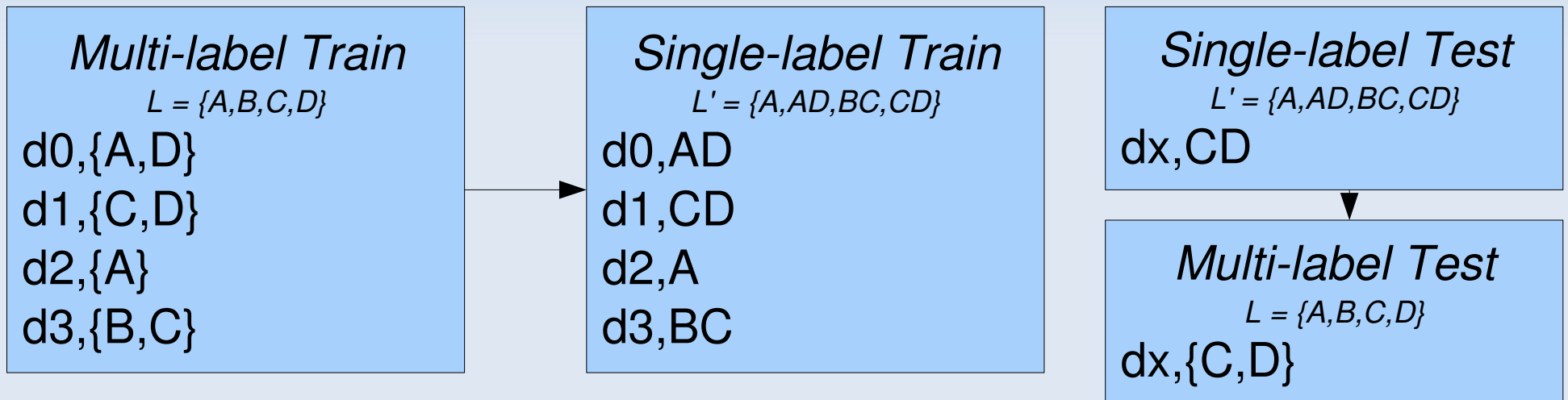
# Combination Method

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# Combination Method

- One decision involves multiple labels
- Each subset becomes a single label



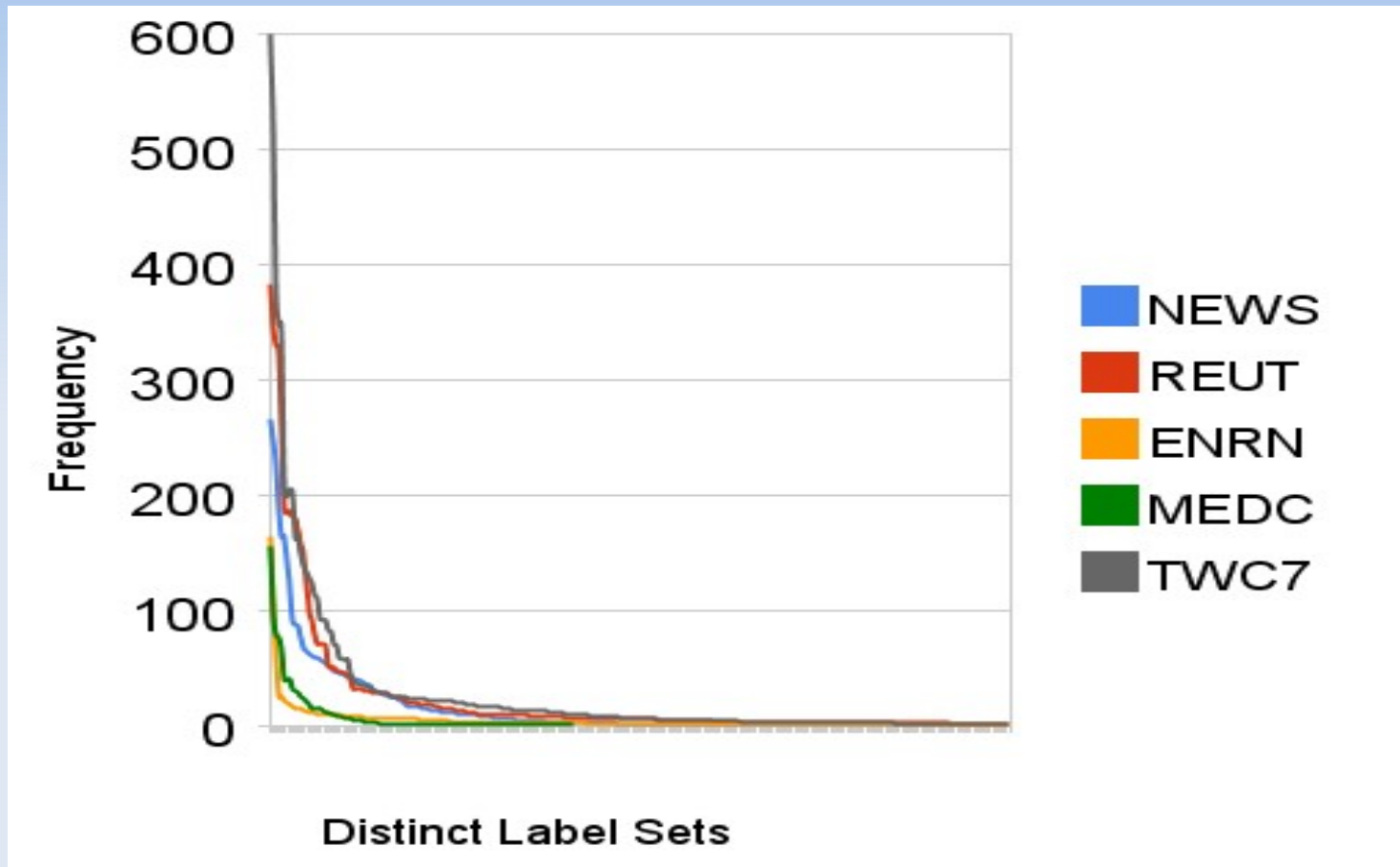
- May generate too many single labels
- Can only predict combinations seen in the training set



# A Pruned Sets Method (PS)

- Binary Method
  - Assumes label independence
- Combination Method
  - Takes into account combinations
  - Can't adapt to new combinations
  - High complexity (~ distinct label sets)
- Pruned Sets Method
  - Use *pruning* to focus on *core* combinations

# A Pruned Sets Method (PS)



## Concept:

- Prune away and break apart infrequent label sets
- Form new examples with more frequent label sets

# A Pruned Sets Method (PS)

E.g. 12 examples, 6 combinations

```
d01,{Animation,Family}  
d02,{Musical}  
d03,{Animation,Comedy }  
d04,{Animation,Comedy}  
d05,{Musical}  
d06,{Animation,Comedy,Family,Musical}  
d07,{Adult}  
d08,{Adult}  
d09,{Animation,Comedy}  
d10,{Animation,Family}  
d11,{Adult}  
d12,{Adult,Animation}
```

# A Pruned Sets Method (PS)

## 1.Count label sets

E.g. 12 examples, 6 combinations

d01,{Animation,Family}  
d02,{Musical}  
d03,{Animation,Comedy }  
d04,{Animation,Comedy}  
d05,{Musical}  
d06,{Animation,Comedy,Family,Musical}  
d07,{Adult}  
d08,{Adult}  
d09,{Animation,Comedy}  
d10,{Animation,Family}  
d11,{Adult}  
d12,{Adult,Animation}

{Animation,Comedy}	3
{Animation,Family}	2
{Adult}	3
{Animation,Comedy,Family,Musical}	1
{Musical}	2
{Adult,Animation}	1

# A Pruned Sets Method (PS)

1.Count label sets

**2.Prune infrequent sets (e.g. count < 2)**

{Animation,Comedy}	3
{Animation,Family}	2
{Adult}	3
{Animation,Comedy,Family,Musical}	1
{Musical}	2
{Adult,Animation}	1

E.g. 12 examples, 6 combinations

d01,{Animation,Family}  
d02,{Musical}  
d03,{Animation,Comedy }  
d04,{Animation,Comedy}  
d05,{Musical}  
d07,{Adult}  
d08,{Adult}  
d09,{Animation,Comedy}  
d10,{Animation,Family}  
d11,{Adult}

d12,{Adult,Animation}  
d06,{Animation,Comedy,Family,Musical}

Information loss!

# A Pruned Sets Method (PS)

- 1.Count label sets
- 2.Prune infrequent sets (e.g. count < 2)
- 3.Break up infrequent sets into frequent sets (e.g. count >= 2)**

{Animation,Comedy}	3
{Animation,Family}	2
{Adult}	3
{Animation,Comedy,Family,Musical}	1
{Musical}	2
{Adult,Animation}	1

E.g. 12 examples, 6 combinations

d01,{Animation,Family}  
d02,{Musical}  
d03,{Animation,Comedy }  
d04,{Animation,Comedy}  
d05,{Musical}  
d07,{Adult}  
d08,{Adult}  
d09,{Animation,Comedy}  
d10,{Animation,Family}  
d11,{Adult}

d12,{Adult,Animation}  
*d12,{Adult}*  
d06,{Animation,Comedy,Family,Musical}  
*d06,{Animation,Comedy}*  
*d06,{Animation,Family}*  
*d06,{Musical}*

# A Pruned Sets Method (PS)

- 1.Count label sets
- 2.Prune infrequent sets (e.g. count < 2)
- 3.Break up infrequent sets into frequent sets (e.g. count  $\geq 2$ )

## 4.Decide which subsets to reintroduce

**(!) Too many (esp. small) sets will:**

- 'dillute' the dataset with single-labels
- vastly increase the training set size

i.e. frequent item sets not desirable

{Animation,Comedy}	3
{Animation,Family}	2
{Adult}	3
{Animation,Comedy,Family,Musical}	1
{Musical}	2
{Adult,Animation}	1

E.g. 12 examples, 6 combinations

d01,{Animation,Family}  
d02,{Musical}  
d03,{Animation,Comedy }  
d04,{Animation,Comedy}  
d05,{Musical}  
d07,{Adult}  
d08,{Adult}  
d09,{Animation,Comedy}  
d10,{Animation,Family}  
d11,{Adult}

d12,{Adult,Animation}  
*d12,{Adult}*  
d06,{Animation,Comedy,Family,Musical}  
*d06,{Animation,Comedy}*  
*d06,{Animation,Family}*  
*d06,{Musical}*

# A Pruned Sets Method (PS)

- 1.Count label sets
- 2.Prune infrequent sets (e.g. count < 2)
- 3.Break up infrequent sets into frequent sets (e.g. count  $\geq 2$ )

## 4.Decide which subsets to reintroduce

### Strategies:

- A. Keep the top  $n$  subsets  
(ranked by *number of labels and count*)  
-or-
- B. Keep all subsets of size greater than  $n$

{Animation,Comedy}	3
{Animation,Family}	2
{Adult}	3
{Animation,Comedy,Family,Musical}	1
{Musical}	2
{Adult,Animation}	1

E.g. 12 examples, 6 combinations

d01,{Animation,Family}  
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d07,{Adult}  
d08,{Adult}  
d09,{Animation,Comedy}  
d10,{Animation,Family}  
d11,{Adult}

d12,{Adult,Animation}  
*d12,{Adult}*  
d06,{Animation,Comedy,Family,Musical}  
*d06,{Animation,Comedy}*  
*d06,{Animation,Family}*  
*d06,{Musical}*



# A Pruned Sets Method (PS)

- 1.Count label sets
- 2.Prune infrequent sets (e.g. count < 2)
- 3.Break up infrequent sets into frequent sets (e.g. count  $\geq$  2)
- 4.Decide which subsets to reintroduce
- 5.Add new instances**

{Animation,Comedy}	3
{Animation,Family}	2
{Adult}	3
{Animation,Comedy,Family,Musical}	1
{Musical}	2
{Adult,Animation}	1

E.g. 12 examples, 6 combinations

d01,{Animation,Family}  
d02,{Musical}  
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d10,{Animation,Family}  
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d12,{Adult,Animation}  
*d12,{Adult}*  
d06,{Animation,Comedy,Family,Musical}  
*d06,{Animation,Comedy}*  
*d06,{Animation,Family}*  
*d06,{Musical}*

# A Pruned Sets Method (PS)

- 1.Count label sets
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- 5.Add new instances
- 6.*Use Combination Method transformation*

E.g. **15** examples, **4** combinations

```
d01,{Animation,Family}
d02,{Musical}
d03,{Animation,Comedy}
d04,{Animation,Comedy}
d05,{Musical}
d07,{Adult}
d08,{Adult}
d09,{Animation,Comedy}
d10,{Animation,Family}
d11,{Adult}
d06,{Animation,Comedy}
d06,{Animation,Family}
d12,{Adult}
```

{Animation,Comedy}	4
{Animation,Family}	3
{Adult}	4
{Musical}	2

# A Pruned Sets Method (PS)

- 1.Count label sets
- 2.Prune infrequent sets (e.g. count < 2)
- 3.Break up infrequent sets into frequent sets (e.g. count >= 2)
- 4.Decide which subsets to reintroduce
- 5.Add new instances
- 6.*Use Combination Method transformation*

- Accounts for label relationships
- Reduced complexity
- Cannot form new combinations (e.g. {Animation,Family,Musical})

{Animation,Comedy}	4
{Animation,Family}	3
{Adult}	4
{Musical}	2

E.g. **15** examples, **4** combinations

```
d01,{Animation,Family}
d02,{Musical}
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d08,{Adult}
d09,{Animation,Comedy}
d10,{Animation,Family}
d11,{Adult}
d06,{Animation,Comedy}
d06,{Animation,Family}
d12,{Adult}
```

# Ensembles of Pruned Sets (E.PS)

Creating new label set classifications

1. Train an Ensemble of PS e.g. Bagging (introduces variation!)

PS

PS

PS

PS

PS

PS

# Ensembles of Pruned Sets (E.PS)

## Creating new label set classifications

1. Train an Ensemble of PS e.g. Bagging (introduces variation!)
2. **Get predictions**

PS	{Musical}
PS	{Animation, Family}
PS	{Animation, Comedy}
PS	{Animation, Family}
PS	{Musical}
PS	{Musical}

# Ensembles of Pruned Sets (E.PS)

## Creating new label set classifications

1. Train an Ensemble of PS e.g. Bagging (introduces variation!)
2. Get predictions
3. **Calculate a score**

Musical:	3	(0.33)
Animation:	3	(0.33)
Family:	2	(0.22)
Comedy:	1	(0.11)

PS	{Musical}
PS	{Animation, Family}
PS	{Animation, Comedy}
PS	{Animation, Family}
PS	{Musical}
PS	{Musical}

# Ensembles of Pruned Sets (E.PS)

## Creating new label set classifications

1. Train an Ensemble of PS e.g. Bagging (introduces variation!)
2. Get predictions
3. Calculate a score
4. **Form a classification set**

**dx, {Animation, Family, Musical}**

Musical:	3 (0.33)
Animation:	3 (0.33)
Family:	2 (0.22)
Comedy:	1 (0.11)

Threshold = 0.15
------------------

PS	{Musical}
PS	{Animation, Family}
PS	{Animation, Comedy}
PS	{Animation, Family}
PS	{Musical}
PS	{Musical}

# Ensembles of Pruned Sets (E.PS)

## Creating new label set classifications

1. Train an Ensemble of PS e.g. Bagging (introduces variation!)
2. Get predictions
3. Calculate a score
4. Form a classification set

**dx, {Animation, Family, Musical}**

→ Can form new combinations

Musical:	3	(0.33)
Animation:	3	(0.33)
Family:	2	(0.22)
Comedy:	1	(0.11)

Threshold = 0.15
------------------

PS

{Musical}

PS

{Animation, Family}

PS

{Animation, Comedy}

PS

{Animation, Family}

PS

{Musical}

PS

{Musical}

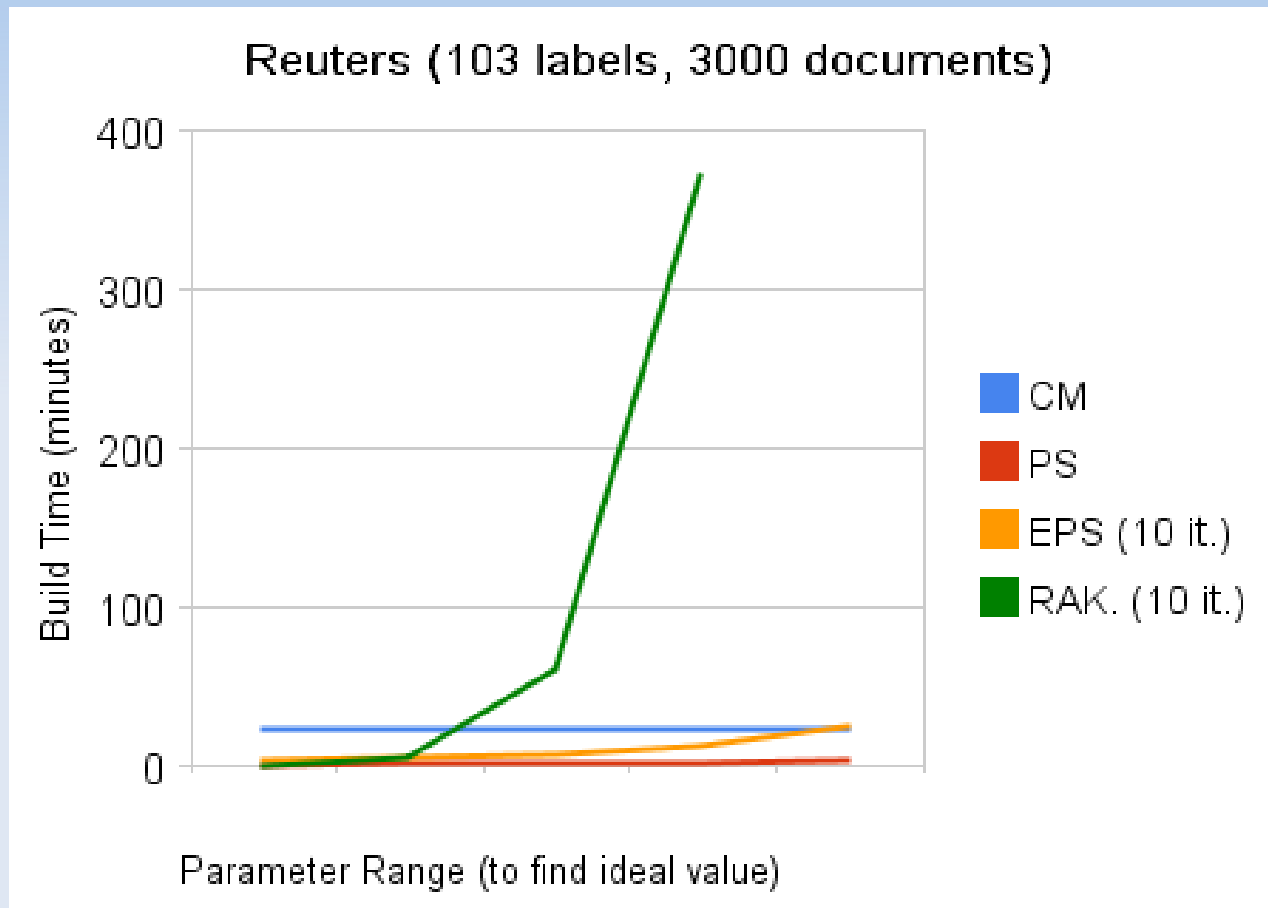


# Results – F1 Measure

D.SET	size /	#lbls /	avg.lbls	BM	[CM]	PS	E.PS	RAK.
<i>Scene</i>	2407	6	1.1	<i>0.671</i>	0.729	0.730	<b>0.752</b>	0.735
<i>Medical</i>	978	45	1.3	<b>0.791</b>	0.767	0.766	0.764	0.784
<i>Yeast</i>	2417	14	4.2	0.630	0.633	0.643	<b>0.665</b>	<b>0.664</b>
<i>Enron</i>	1702	53	3.4	0.504	0.502	0.520	<b>0.543</b>	<b>0.543</b>
<i>Reuters</i>	6000	103	1.5	<i>0.421</i>	0.482	0.496	<b>0.499</b>	<i>0.418</i>

- Combination Method (CM) improves Binary Method (BM)
- Puned Sets method (PS) improves Combination Method (CM)
  - Except *Medical*: maybe label relationships not as important
- E.PS is best overall.
- RAKEL ~ EPS similar
- What about complexity?

# Complexity – Build Time



- RAKEL may not be able to find ideal parameter value
- '*Worst case*' scenarios are similar, but different in practice

# Complexity – Memory Use

## Reuters Dataset

- **PS** transformation: ~**2,500** instances
- **EPS** transformation: ~**25,000** instances (for 10 iterations)
- **RAKEL** transformation: **3,090,000** instances (for 10 iterations)

Number of instances generated during the *Problem Transformation* procedure for *most complex* parameter setting

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# On-line Multi-label Classification

Many multi-label data sources are *on-line*:

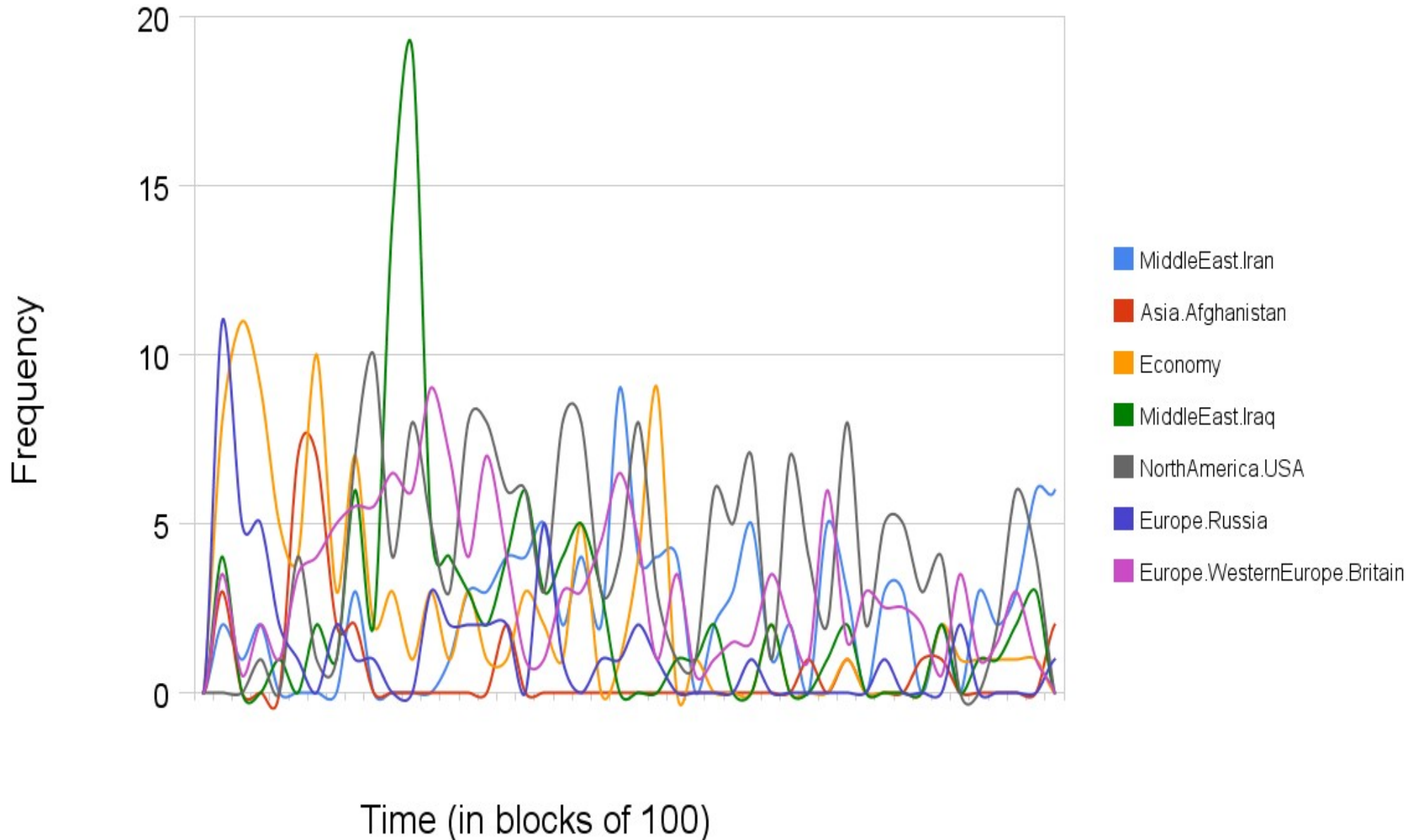
- New instances incoming
- Data can be time ordered
- Possibly large collections
- Concept drift

An on-line multi-label algorithm should be:

- Adaptive
- Efficient

# On-line Multi-label Classification

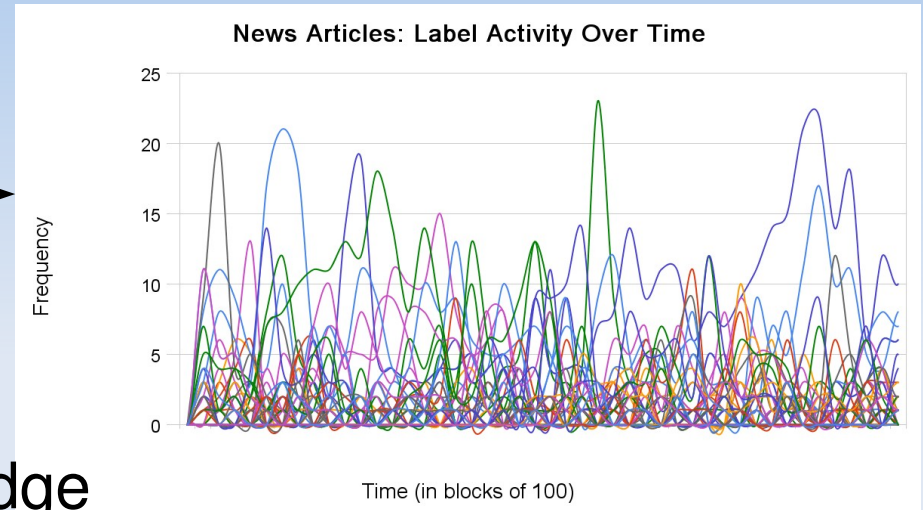
## News Articles: Label Activity Over Time



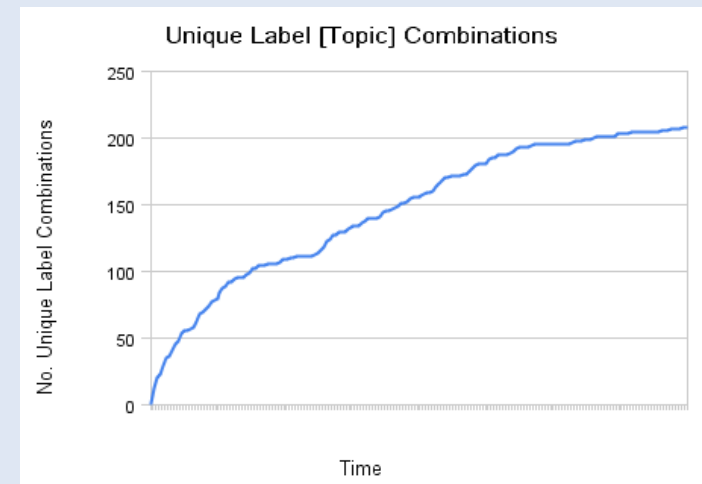
# Multi-label Concept Drift

## Measuring concept drift

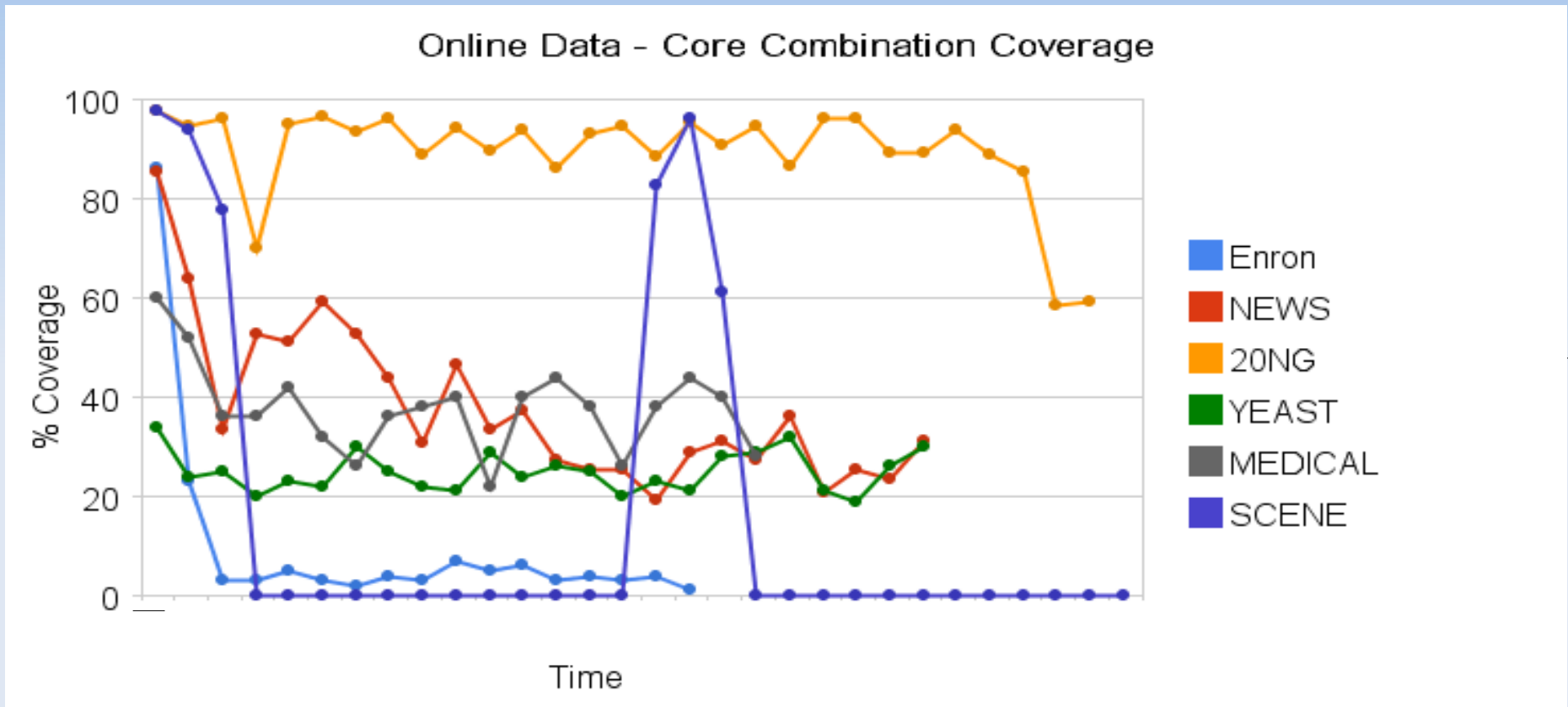
- Observing indiv. labels? ▶
  - Complicated (may be 1000's of labels)
  - May need domain knowledge



- Counting distinct label *sets*? →
  - Doesn't tell us much
- PS Transformation?
  - Focus on core combinations



# Multi-label Concept Drift



20NG; News; Enron –(*On-line data*)– Slow; medium; rapid **concept drift**

YEAST – *Randomised*

SCENE – *Ordered Train/Test Split*

MEDICAL – *???*

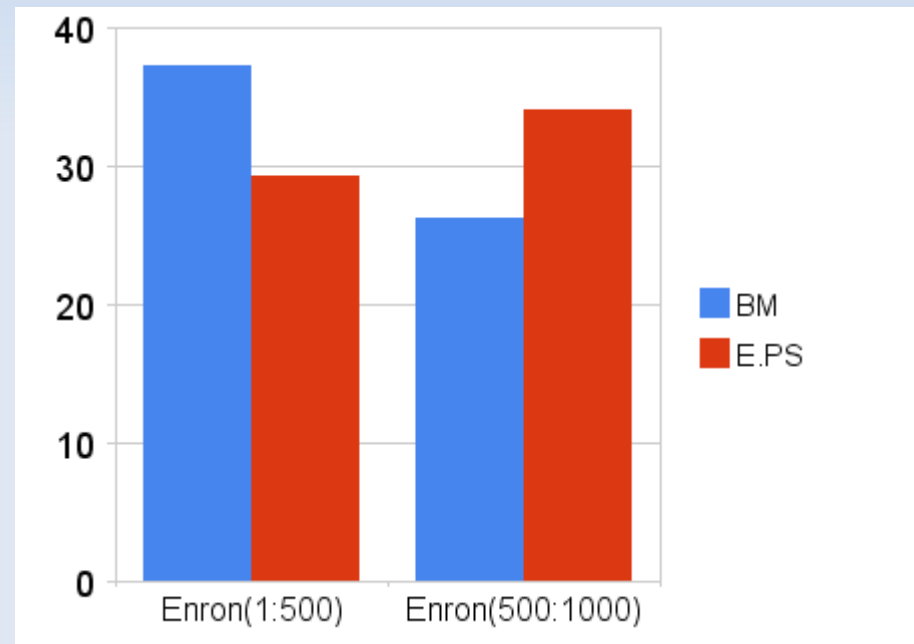
1. PS transformation on first 50 instances
2. Measure the % coverage
3. Measure on the next 50, and etc ..



# Preliminary Results

- 'On-line' Binary Method vs E.PS
  - Model(s) built on 100 instances
  - Thresholds updated every instance
  - Model(s) rebuilt every 25 instances

Enron Dataset - Subsets - Accuracy



# Summary

- Multi-label Classification
- Problem Transformation
  - Binary Method (BM), Combination Method (CM)
- Pruned Sets (PS) and Ensembles of PS (E.PS)
  - Focus on core label relationships via pruning
  - Outperforms standard and state-of-the-art methods
- Multi-label Classification in an On-line Context
  - Naive methods (eg. BM) can perform better than EPS in an on-line context (future work!)

# Questions

?